

Name:

Date:

Topic:

Class:

Main Ideas/Questions

Notes/Examples

PASCAL'S TRIANGLE

Pascal's triangle was a pattern of numbers that was discovered in the 13th century. Each number in Pascal's triangle is the sum of the two numbers diagonally above it. All outside numbers are 1.

Complete rows 4 and 5 of Pascal's triangle below:

Row 0 →

1

Row 1 →

1

1

Row 2 →

1

2

1

Row 3 →

1

3

3

1

Row 4 →

Row 5 →

*Expanding Binomials*Expand the binomial $(a + b)^3$:

What do you notice about the coefficients?

THE BINOMIAL THEOREMIf n is a natural number, then $(a + b)^n =$

$${}_n C_0 \cdot a^n b^0 + {}_n C_1 \cdot a^{n-1} b^1 + {}_n C_2 \cdot a^{n-2} b^2 + \dots + {}_n C_n \cdot a^0 b^n = \sum_{k=0}^n {}_n C_k \cdot a^{n-k} b^k$$

*Examples***Directions:** Use the binomial theorem to expand each binomial.

1. $(a + b)^5$

2. $(x + y)^7$

	3. $(c + d)^{10}$
Coefficients Other than 1	4. $(x - 3)^6$
	5. $(2m + n)^7$
	6. $(k + 2)^8$
	7. $(3p - 2q)^5$
Observations	<p>In the binomial expansion of $(a + b)^n$:</p> <ul style="list-style-type: none"> • The total number of terms is always _____. • The exponent of a in the first term is _____. • The exponent of b in the last term is _____. • The exponent of a _____ from left to right. • The exponent of b _____ from left to right. • The sum of the exponents in each term is _____. • The coefficients are _____ and follow the _____ row of _____.