## AP Statistics Chapter 12: More about Regression

## 12.1 - Inference for Linear Regression

## Sample Computer Output for a Linear Data Analysis

| Predictor | Coef | SE Coef | $T$ | $P$ |
| :--- | :--- | :--- | :--- | :--- |
| Constant | 7.0647 | 0.2672 | 26.44 | 0.000 |
| Years since | 1970 | 0.36583 | 0.01048 | 34.91 |
| S $=0.544467$ | R-Sq $=98.9 \%$ | R-Sq (adj) $=98.8 \%$ |  |  |

- For the above, the linear equation is $y=7.0647+0.36583 x$
- The Standard Error of the slope $\left(\mathrm{SE}_{\mathrm{b}}\right)=0.01048$
- $S=$ the Standard Deviation of the Residuals. Since $S=0.544$, predictions of $y$ from $x$ based on this regression model will be off by an average of about 0.544.


## Confidence Interval for the Slope of a Regression Line

The confidence interval for $b$ has the familiar form

```
statistic }\pm\mathrm{ (critical value) · (standard deviation of statistic)
```

The $t$ Interval for the slope $\beta: \quad b \pm t^{*} S E_{b}$
Where $b$ is the slope, $S E_{b}$ is the standard error of the slope, and $t$ is the critical value with $\mathrm{df}=\mathrm{n}-2$.

## Performing a Significance Test for the Slope

$\mathbf{H}_{0}: \beta=\beta_{0}$ (some hypothesized value - often 0)
$\mathbf{H}_{\mathbf{a}}$ : either $\beta<\beta_{0}$ or $\beta>\beta_{0}$ or $\beta \neq \beta_{0}$
Test Statistic: $t=\frac{b-\beta_{0}}{S E_{b}} \quad$ P-Value: Use the $t$ distribution with $\mathrm{df}=n-2$

## 12.2 - Transformations to Achieve Linearity

| Finding an Exponential Model for Data | Finding a Power Model for Data |
| :---: | :--- |
| Form: $y=A(B)^{x}$ | Form: $y=A(x)^{B}$ |
| Transformation: $(x, \log y)$ | Transformation: $(\log x, \log y)$ |
| Process: | Process: |
| 1. LinReg $(x, \log y)$ | 1. LinReg $(\log x, \log y)$ |
| 2. Resulting line is $y=a+b x$ | 2. Resulting $\operatorname{line}$ is $y=a+b x$ |
| 3. Let $A=10^{a}$ and $B=10^{b}$ | 3. Let $A=10^{a}$ and $B=b$ |

